Simultaneous Identification and Control for Hybrid Energy Storage System Using Model Predictive Control and Active Signal Injection

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Abstract—A battery/supercapacitor hybrid energy storage system (HESS) is overactuated in the sense that there are two power sources providing a single power output. This feature of HESS is exploited in this article to simultaneously achieve accurate identification of the battery states/parameters and high system efficiency. By actively injecting current signals, the state of charge and state of health, together with other battery parameters, can be identified sequentially. Sufficient richness in the input (i.e., battery current) is necessary to ensure identification accuracy. Since signal richness for identification can be in conflict with efficient operation, a novel model predictive control (MPC) strategy is used to simultaneously consider both objectives to determine the optimal power distribution between supercapacitor and battery. The tradeoff between identification accuracy and system efficiency is investigated. Simulation results show that the proposed MPC can significantly improve identification accuracy at the expense of a slight decrease in system efficiency when compared to the baseline MPC, which does not consider the signal richness. Therefore, it is validated that the proposed MPC can effectively achieve simultaneous identification and efficient operation.

Index Terms—Hybrid energy storage system (HESS), lithium-ion battery, model predictive control (MPC), overactuated nature, state of charge (SoC)/state of health (SoH) identification.

Manuscript received February 4, 2019; revised August 12, 2019; accepted October 27, 2019. Date of current version July 14, 2020. This work was supported by U.S. Office of Naval Research under Grant N00014-16-1-3108 and Grant N00014-18-2330. (Corresponding author: Jun Hou.)

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NOMENCLATURE

- \( a \): OCV–SoC slope (V%).
- \( b \): Constant of linearized OCV–SoC curve (V).
- \( C_{SC} \): SC capacitance (F).
- \( C_l \): Capacitance of \( RC \) pair (F).
- \( i_{b} \): Battery current (A).
- \( i_{b,\text{max}} \): Maximum battery current (A).
- \( i_{b,\text{min}} \): Minimum battery current (A).
- \( I_{ex} \): Amplitude of the injected current (A).
- \( I_{ex,\text{max}} \): Maximum injected current (A).
- \( I_{ex,\text{min}} \): Minimum injected current (A).
- \( i_{SC} \): Supercapacitor current (A).
- \( i_{SC,\text{max}} \): Maximum supercapacitor current (A).
- \( i_{SC,\text{min}} \): Minimum supercapacitor current (A).
- \( K_0-K_4 \): Coefficients of OCV–SoC curve.
- \( N \): Prediction horizon.
- \( P_{b} \): Battery power (kW).
- \( P_d \): Power demand (kW).
- \( P_{SC} \): Supercapacitor power (kW).
- \( Q_{b} \): Battery capacity (Ah).
- \( R_{b} \): Ohmic resistance of battery (Ω).
- \( R_{b,\text{est}} \): Estimated ohmic resistance (Ω).
- \( R_{SC} \): Supercapacitor resistance (Ω).
- \( R_{t} \): Resistance of \( RC \) pair (Ω).
- \( s \): Complex Laplace variable.
- \( SoC_b \): Battery SoC (%).
- \( SoC_{b,\text{max}} \): Maximum battery SoC (%).
- \( SoC_{b,\text{min}} \): Minimum battery SoC (%).
- \( SoC_{SC} \): Supercapacitor SoC (%).
- \( SoC_{SC,\text{max}} \): Maximum supercapacitor SoC (%).
- \( SoC_{SC,\text{min}} \): Minimum supercapacitor SoC (%).
- \( t \): Time (s).
- \( t_0 \): Start time (s).
- \( T_s \): Sampling time (s).
- \( v_b \): Battery terminal voltage (V).
- \( v_C \): Voltage over the \( RC \) pair (V).
- \( v_{OC} \): Open-circuit voltage of battery (V).
- \( v_{SC} \): Open-circuit voltage of supercapacitor (V).
- \( v_{SC,\text{max}} \): Maximum voltage of supercapacitor (V).
PARAMETER identification and system optimization are often conflicting objectives, with identification requiring persistently exciting inputs for parameter convergence [1], while system optimization objectives generally minimize a predefined cost function that does not generate persistently exciting inputs. While these conflicting objectives cannot be simultaneously achieved for most systems overactuated systems in which the number of inputs is greater than the number of outputs [2] can be exploited for SIC. Overactuated systems provide an opportunity to introduce excitation for parameter identification in such a way that it does not perturb regulated outputs [1].

Similar work, which trades off parameter identification and output regulation objectives can be found in the literature. For example, Reed et al. exploited the overactuation of permanent magnet synchronous machines (PMSMs) to achieve parameter identification and torque regulation objectives simultaneously [3]. Hasanzadeh et al. [4] also focused on the PMSM and estimated the rotor resistance by injecting a relatively low-frequency carrier signal, and then the overactuation feature was utilized to minimize the torque ripple by the carrier signal. Chen and Wang [5] used the additional degrees of freedom in an electric vehicle with independent motors to provide additional excitation for accurate tire-road friction coefficient estimation. Similarly, Leve and Jah exploited the “null motion” of an overactuated spacecraft to add excitation for parameter identification without disturbing the control objective [6].

The battery/SC HESS has been widely used in transportation [7] and grid [8] applications, given that the adoption of SC is an effective solution to prolong battery lifetime [9]. HESS is an overactuated system since there are two inputs, i.e., the output power of SC and battery, and a single output, i.e., the demand power required by the load. Therefore, HESS offers an additional degree of freedom which can be potentially utilized to improve parameter identification performance [10]. We point out that the overactuated nature of HESS is worthy of investigation because accurate identification of parameters/states, such as battery SoC and SoH, plays an important role in ensuring reliable and efficient operation [11]. However, most existing studies of HESS focus on topology optimization [12], component sizing [13], and design of the energy management strategy [14]. The overactuated nature of HESS has been neglected.

The SC can be represented by a simple model and, therefore, simply characterized [15]. However, the concurrent identification of battery SoC/SoH together with its model parameters, which are significantly influenced by battery degradation and operating conditions [16], is still challenging considering measurement noise and model inaccuracy [17]. It has been proven that identification accuracy can be impaired when data without rich information is used [18], even though most existing studies use data indiscriminately [19]. Recently, more attention has been paid to the impact of data on the identification performance of battery parameters. Lin and Stefanopoulou [20] and Klingberg et al. [21] used the CR bound to quantify the influence of data on identification accuracy. Rothenberger et al. [22] optimized the battery current profile to maximize the Fisher information matrix and, therefore, improve identification performance, [23]. The connection between excitation input and SoC estimation error considering sensor bias and variance has also been investigated [24]. It has been shown that the identification performance of a sequential algorithm, which identifies battery parameters and states sequentially by actively injecting current signals, can be significantly improved when compared to the case where all battery parameters and states are estimated concurrently [25].

Even though the aforementioned literatures have pointed out that the current profile significantly influences the identification accuracy of battery parameters/states and it is worthwhile actively injecting optimal signals to battery, none of them have implemented such an algorithm in practical applications. This article extends the framework of the original SIC by considering system efficiency in addition to identification and control objectives.

This is the first article, this article is the first to consider optimization objectives and identification accuracy simultaneously, and realizes active signal injection into the battery to increase the identification accuracy in an overactuated system when the system can normally work in practical conditions.

To actively inject the excitation current, the overactuated feature of HESS, which has been widely used in electric vehicles [12] and all-electric ships [26], is exploited using MPC [27], which has been explored as a framework for SIC [28]–[30]. MPC is used in this article to simultaneously consider the signal richness for identification and HESS efficiency by optimally distributing power between SC and battery. Simulation results show that the proposed MPC can significantly improve identification accuracy at the expense of a slight reduction in system efficiency when compared to a baseline MPC which does not consider signal richness. In addition, the tradeoff between identification accuracy and HESS efficiency is investigated.

This is the first article utilizing the overactuation feature to actively inject signals into a battery in use, thereby significantly improving the estimation accuracy of battery states/parameters. This improvement is crucial to the safe, efficient, and reliable
operation of Lithium-ion batteries. Specifically, the proposed algorithm can avoid the inherent uncertainties involved in the estimation process by compromising with slightly more energy consumption.

The rest of this article is organized as follows. In Section II, simultaneous identification and optimization is introduced and the HESS model is described. In Section III, formulations of the baseline MPC and proposed MPC are presented. Simulation results are provided and analyzed in Section IV. Section V concludes this article.

II. HYBRID ENERGY STORAGE SYSTEM

A. Simultaneous Identification and Control Objective

The HESS under investigation has two power sources (i.e., SC and battery) and provides output power to a single load, as shown in Fig. 1. Thus, the power output of each energy storage can vary while keeping the total output power constant. The overactuated nature of HESS provides a perfect opportunity to address the SIC problem, which ensures that a sufficient condition for accurate parameter identification (i.e., persistently exciting inputs) is maintained in addition to achieving a control objective (e.g., output regulation) [1]. A persistently exciting input is especially important for the battery since it is difficult to simultaneously identify all battery parameters and states [25]. This article considers system efficiency in addition to identification and control objectives. Specifically, an excitation current of a desired frequency is injected to achieve battery parameter/state identification. Then, the signal richness, which has been proven to be linearly proportional to the amplitude of the injected current [17], and the system efficiency are optimized through a weighted-sum method to convert the multi-objective optimization problem (i.e., system efficiency and identification accuracy) into a single-objective optimization problem, while the output power of the HESS is accurately controlled to follow the power demand. While identification and control can be simultaneously achieved without compromise by exploiting the overactuated feature of HESS, identification and optimization are still conflicting objectives for overactuated systems since in general the optimal solutions for maximizing system efficiency do not include an input with sufficient richness for identification. Therefore, the goal of this article is to achieve the best tradeoff between these competing objectives. Note that the proposed SIC is dealing with a time-varying system as the battery parameter is continuously estimated by the sequential algorithm and then fed back to the proposed MPC, which attempts to simultaneously minimize the energy loss and maximize the signal richness.

B. Equivalent Circuit Models for Battery and Supercapacitor

In the proposed SIC framework, the cost function accounts for the power losses of both SC and battery, which are calculated based on ECMs.

The SC ECM can be simplified to an RC circuit, as shown in Fig. 2(a) [10]. The SC OCV, terminal voltage, resistance, and current are denoted as $v_{SC}$, $v_t$, $R_{SC}$, and $i_{SC}$ (positive for discharging and negative for charging), respectively. The SoC of SC is linearly proportional to its OCV and therefore can be easily estimated [12]

$$\text{SOC}_{SC}(t) = \text{SOC}_{SC}(0) - \int_{0}^{t} \frac{i_{SC}(t)}{C_{SC}/v_{SC,max}} dt \tag{1}$$

where $t$ is the time instant, $C_{SC}$ is the SC capacitance, and $v_{SC,max}$ is the SC maximum voltage. In contrast, the ECM for representing the battery dynamics is more complicated. Among all existing models, the first-order ECM, as shown in Fig. 2(b) [31], is widely used in practical applications due to its sufficient accuracy and low computational cost. Therefore, it is also adopted in this paper for battery state/parameter identification.

As shown in Fig. 2(b), the battery terminal voltage is defined as $v_b$ and the battery current is defined as $i_b$. The first-order ECM dynamics can be derived as follows:

$$\begin{cases} i_C = -\frac{1}{R_T} v_C + \frac{1}{R_T} i_b, \\ v_b = v_{OC} - R_s i_b - v_C \tag{2} \end{cases}$$
where $v_C$ is the voltage over the $RC$ pair and $\tau = R_C t$ is the time constant. The OCV–SoC curve can be expressed as follows [32]:

$$v_{OC}(z) = K_0 - \frac{K_1}{z} - K_2 z + K_3 \ln(z) + K_4 \ln(1 - z)$$  (3)

where $K_0$–$K_4$ are the model coefficients and $z$ is the normalized SoC, and the SoC dynamic is given by the following [33]:

$$z = z_0 - \int_{t_0}^{t} \frac{\eta i_b(t)}{Q_b} dt$$  (4)

where $z_0$ is the initial SoC, $\eta$ is the charging/discharging efficiency, $i_0$ is the start time, and $Q_b$ is the battery capacity. For the combined state and parameter estimation problem studied in this article, we assume that the values of $R_\text{s}, R_\text{i},$ and $\tau$ are constant in the estimation process, since they vary much more slowly than the battery SoC [34].

### C. Brief Review of Sequential Algorithm

The identification of battery states (e.g., SoC and SoH) and parameters is an important and difficult task in practical applications, but identification accuracy is limited when identifying all parameters and states simultaneously due to noise and unmodeled dynamics. The sequential algorithm is proposed to solve this problem. Identifying battery parameters/states sequentially by incorporating a high-pass filter and actively injecting current has been proven to significantly improve identification accuracy [25]. The sequential algorithm was designed based on battery dynamic analysis in the frequency domain [25]. To simplify the analysis, (3) is linearized given that the slope of the OCV–SoC curve is constant for most battery chemistries within the normal operating range [35]

$$v_{OC}(t) = a \left( z_0 - \int_{t_0}^{t} \frac{\eta i_b(v)}{Q_b} dv \right) + b$$  (5)

where $a$ and $b$ are the coefficients of the linearized OCV–SoC function. Based on (2)–(5), the battery dynamics in the frequency domain can be derived using the Laplace transform

$$v_b(s) = \left[ \frac{az_0}{s} + \frac{b}{s} \right] - \left[ \frac{a}{s} \frac{\eta i_b(s)}{Q_b} \right] - \left[ R_s i_b(s) \right]$$

$$- \left[ \frac{R_i}{1 + \frac{7}{s}} i_b(s) \right]$$  (6)

where $s$ is the complex Laplace variable. As shown in (6), the battery terminal voltage includes four components, which are dominated by the initial SoC, SoC variation, ohmic resistance, and $RC$ pair, respectively. These four components have significantly different dynamic characteristics, and can be decomposed by incorporating high-pass filters and actively injecting current. Specifically, by using the high-pass filter, the first term associated with the initial SoC can be removed because it is constant. As for the filtered system, when the current frequency is high, the battery voltage is dominated by the ohmic resistance drop. At medium frequency the term associated with the SoC variation can be neglected and the battery voltage is dominated by the ohmic resistance and $RC$ pair. Therefore, the sequential algorithm can be summarized in the following three steps [25].

**Step #1:** By incorporating a high-pass filter and injecting high-frequency current, the ohmic resistance is identified using the EKF.

**Step #2:** The estimated ohmic resistance is used. By incorporating a high-pass filter and injecting medium-frequency current, $R_\text{s}$ and $\tau$ are identified using the EKF.

**Step #3:** The estimated $R_\text{s}, R_\text{i},$ and $\tau$ are adopted. Hence, the SoC and SoH can be simultaneously estimated based on the unfiltered system. A dual EKF, which can identify the states and parameters concurrently, is employed.

### III. SIMULTANEOUS IDENTIFICATION AND CONTROL USING MODEL PREDICTIVE CONTROLLER

MPC is used in this article to solve the SIC problem, deal with constraints, and regulate the HESS output power. The baseline MPC, which does not consider current injection, is first introduced. The baseline MPC is denoted as MPC–, and the states and inputs of MPC– are defined as follows:

$$x(k) = \begin{bmatrix} \text{SoC}_b(k) \\ \text{SoC}_{SC}(k) \end{bmatrix}, u(k) = \begin{bmatrix} i_b \\ i_{SC}(k) \end{bmatrix}.$$  (7)

Note that the control horizon of $i_b$ is chosen to be 1 for a fair comparison with the proposed MPC, which will be described later. The optimization problem of MPC– is formulated as follows:

$$J_{\text{MPC–}}(x(k), u(k)) = \sum_{k=0}^{N} \left[ R_s i_b^2 + R_{\text{SC}} i_{SC}^2(k) \right] + \lambda_1 [v_{\text{SC}}(k) - 0.9 v_{\text{SC,max}}]^2$$  (8)

subject to the constraints

$$\text{SoC}_{b,\text{min}} \leq \text{SoC}_b \leq \text{SoC}_{b,\text{max}},$$

$$\text{SoC}_{SC,\text{min}} \leq \text{SoC}_{SC} \leq \text{SoC}_{SC,\text{max}},$$

$$i_{b,\text{min}} \leq i_b \leq i_{b,\text{max}},$$

$$i_{SC,\text{min}} \leq i_{SC} \leq i_{SC,\text{max}},$$

$$\sum_{k=0}^{N} |P_d - P_b(k) - P_{SC}(k)| \leq \varepsilon,$$

$$x(k + 1) = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} x(k) - \begin{bmatrix} T_{b,0} Q_b \\ 0 \end{bmatrix} \frac{T_r}{v_{\text{SC,max}} C_{\text{SC}}} u(k)$$

where $J_{\text{MPC–}}$ is the cost function of MPC–, $N$ is the prediction horizon, $\lambda_1$ is the weighting parameter that allows us to put a different emphasis on each objective, $k$ is the time instant, $v_{\text{SC}}$ is the SC voltage, $v_{\text{SC,max}}$ is the maximum voltage of SC, $\text{SoC}_{b,\text{min}}$ and $\text{SoC}_{SC,\text{min}}$ (SoC$_{SC,\text{max}}$) are the lower (upper) boundaries of the SoC of the battery and SC, respectively, $i_{b,\text{min}}$ and $i_{b,\text{max}}$, and $i_{SC,\text{min}}$ (iSC$_{\text{max}}$) are the lower (upper) boundaries of the current of the battery and SC, respectively, $P_b$ and $P_{\text{SC}}$ are the battery and SC power, $P_d$ is the power demand, $\varepsilon$ is a small
allowable error for the output power regulation, $Q_b$ is the battery capacity, $C_{SC}$ is the SC capacitance, and $T_s$ is the sampling time (e.g., 1 s for MPC−). In the cost function of baseline MPC, HESS power loss and SC usage are concurrently considered.

The reference value of SC SoC is set to 0.9 to give the SC some storage capacity to absorb regenerative braking energy [14]. The cost term associated with the SC SoC reference aims to address the limitation of a short predictive horizon and use the SC more effectively [26]. Note that $P_d$ is assumed to be constant in the prediction horizon, meaning that the power demand prediction is not considered in this study. The SC SOC is strictly controlled above 50% because the efficiency of power conversion becomes poor when the SC voltage is low. In addition, the battery voltage is assumed to be constant to simplify the calculation because the variation of battery voltage is generally small in its normal operating range [14]. Output regulation is realized by a nonlinear constraint. In addition, the RC pair is neglected in the calculation of battery power loss, since the time constant of the Lithium-ion battery in this study is more than 15 s, while the sampling period of MPC is less than 1 s. Therefore, the battery current mainly flows through the capacitor in the RC pair and the dynamics associated with the RC pair can be neglected.

A sinusoidal battery current, which is frequently used for parameter estimation, is injected for the sequential algorithm to identify battery parameters/states

$$i_{ex}(t) = I_{ex} \cos(2\pi ft)$$

where $i_{ex}$ is the injected current, $I_{ex}$ is the current amplitude, and $f$ is the current frequency. It has been proven that the identification accuracy is proportional to the amplitude of excitation current [10]. Hence, the proposed MPC, denoted as MPC+, not only ensures that the excitation current of desired frequencies are injected but also takes the signal magnitude (i.e., $I_{ex}$) into consideration. The state of MPC+ is the same as that of MPC−, and the amplitude of excitation current is added to the inputs of MPC+

$$u(k) = \begin{bmatrix} i_b \\ i_{SC}(k) \end{bmatrix}.$$  

(10)

The control horizons of $i_b$ and $I_{ex}$ are both chosen as 1 s to ensure the successful injection of excitation current. Otherwise, the injected signal will be compensated by $i_b$ and disappear in the battery current profile, since minimizing the system power loss and increasing the signal richness for identification are inherently conflicting objectives. Note that $i_b$ is also set to be constant in the prediction horizon in the cost function of the baseline MPC, as shown in (8), in order to have a fair comparison.

The optimization problem of MPC+ is defined as follows:

$$J_{MPC+}(x(k), u(k)) = \sum_{k=0}^{N} \left[ \hat{R}_s(i_b + I_{ex} \cos(2\pi fT_s k))^2 
+ R_{SC}i_{SC}^2(k) 
+ \lambda_1[v_{SC}(k) - 0.9v_{SC, max}]^2 + \lambda_2 \frac{1}{I_{ex}} \right]$$

(11)

subject to the constraints

$$\text{SoC}_{b,\min} \leq \text{SoC}_b \leq \text{SoC}_{b,\max},$$

$$\text{SoC}_{SC,\min} \leq \text{SoC}_{SC} \leq \text{SoC}_{SC,\max},$$

$$I_b, \min \leq i_b \leq I_b,\max,$$

$$I_{SC,\min} \leq |I_{SC} | \leq I_{SC,\max},$$

$$I_{ex,\min} \leq i_{ex} \leq I_{ex,\max},$$

$$\sum_{k=0}^{N} |P_d - P_b(k) - P_{SC}(k)| \leq \varepsilon,$$

$$x(k+1) = \begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix} x(k)$$

- $\begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix}$

where $J_{MPC+}$ is the cost function of MPC+, $\lambda_2$ is the weighting parameter for the signal amplitude, $\hat{R}_s$ is the estimated ohmic resistance, and $I_{ex,\min}$ ($I_{ex,\max}$) is the lower (upper) boundary of the excitation current amplitude. The sampling time of MPC+ depends on the frequency of the injected signal, and $T_s$ is set to 0.2 and 1 s for injecting current signals of 0.5 and 0.05 Hz, respectively.

**Remark:** Note that the estimated resistance is also used in the optimization. When compared to the traditional estimation and optimization formulations [27], the advantage of this novel SIC framework is that the persistently exciting inputs for the parameter estimation are guaranteed by the proposed MPC. Therefore, the estimated parameter will converge to its actual value, and in turn, it can be used in the optimization to improve system performance.

**IV. SIMULATION RESULTS**

**A. System Optimization**

A power demand profile corresponding to a typical bus driving cycle shown in Fig. 3 is adopted, given that HESS has been widely used in transportation applications [12]. Therefore, the sizes of the battery and SC packs are scaled to those of an
TABLE I
SPECIFICATION FOR THE MPC FORMULATION

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Prediction horizon $N$</td>
<td>10</td>
</tr>
<tr>
<td>Resistance of the battery pack $R_b$ (mΩ)</td>
<td>64</td>
</tr>
<tr>
<td>Resistance of the SC pack $R_{SC}$ (mΩ)</td>
<td>43</td>
</tr>
<tr>
<td>Battery pack capacity $Q_b$ (Ah)</td>
<td>500</td>
</tr>
<tr>
<td>SC pack capacitance $C_p$ (F)</td>
<td>63</td>
</tr>
<tr>
<td>Battery pack voltage (V)</td>
<td>384</td>
</tr>
<tr>
<td>Maximum voltage of SC pack $v_{SC,max}$ (V)</td>
<td>625</td>
</tr>
<tr>
<td>Battery current boundaries $I_{max}$ (A)</td>
<td>-200/-200</td>
</tr>
<tr>
<td>SC current boundaries $I_{SC,min}/I_{SC,max}$ (A)</td>
<td>-240/240</td>
</tr>
<tr>
<td>Battery SoC boundaries $SoC_{min}/SoC_{max}$ (%)</td>
<td>20/90</td>
</tr>
<tr>
<td>SC SoC boundaries $SoC_{SC,min}/SoC_{SC,max}$ (%)</td>
<td>50/90</td>
</tr>
<tr>
<td>Boundaries of excitation current amplitude $I_{max}/I_{e,max}$ (A)</td>
<td>5/10</td>
</tr>
<tr>
<td>Tolerance of the output power regulation $e$ (kW)</td>
<td>0.1</td>
</tr>
</tbody>
</table>

Fig. 4. Power split results of baseline MPC without current injection.

The specifications of HESS and MPC–/MPC+ are listed in Table I. The weighting parameters $\lambda_1$ and $\lambda_2$ are determined through trial-and-error, and $\lambda_1$ is set to 4 for the MPC– to achieve optimal performance (i.e., minimum energy loss). The “fmincon” MATLAB function is used to solve all MPC problems in this article [36].

As shown in Fig. 4, MPC– effectively distributes the power between the SC and battery, while the demand power is accurately followed by the HESS. The SoC of SC fluctuates in a wide range to supply/absorb high power demands, meaning that the SC is effectively used. The battery only supplies low and “constant” power, therefore its life span can be significantly prolonged. The energy consumption of HESS during the entire driving cycle is 9899.76 kJ.

For the proposed MPC+, a sinusoidal current of 0.5 Hz is actively injected first to identify the ohmic resistance. The sampling time is set to 0.2 s considering the frequency of the injected current. Based on the simulation results, the weighting parameters $\lambda_1$ and $\lambda_2$ in the cost function of MPC+ are set to 20 and 1000, respectively. Note that $\lambda_1$ is increased in the MPC+ based on trial-and-error when compared to the one in MPC– (i.e., 4). In both MPC– and MPC+, $\lambda_1$ and $\lambda_2$ are tuned manually to achieve optimal performance in order to enable a fair comparison between different algorithms. Under the proposed MPC+, the power demand is well followed, indicating a satisfactory output regulation performance as shown in Fig. 5. In addition, the desired excitation is successfully injected in the battery current profile, and the fluctuations in the SC current profile compensate the negative influence of the injected current on the output regulation. Therefore, the SIC is well addressed by the proposed MPC+. As for the SIC, the simulation result shows that the energy consumption of HESS during the entire cycle is 9940.83 kJ, revealing that MPC+ has a compromise of 0.4% increase when compared to MPC–. The identification results and the tradeoff between identification and loss minimization, which verify the proposed MPC+ can effectively perform SIC, will be presented in the sequel.

Simulation results which involve actively injecting a current of 0.05 Hz are shown in Fig. 6. The sampling time is increased to 1 s, and the weighting parameters $\lambda_1$ and $\lambda_2$ in the cost function of MPC+ are set to 4 and 200, respectively. The energy consumption of HESS is 9936.85 kJ, which has a 0.37% increase when compared to the MPC–.

To better present the excitation current injection, the characteristics of the current profiles corresponding to different cases are analyzed in the frequency domain using the fast Fourier transform, as shown in Fig. 7. This shows that the desired excitation current, which is necessary for the sequential algorithm, therefore can be successfully injected by the proposed MPC+. It is validated that the proposed MPC+ can ensure that persistently
exciting signals with the desired frequency content always exist.
In comparison, for the baseline MPC, the persistently exciting
condition cannot be guaranteed. For example, when the power
demand is 0, both the battery current and the supercapacitor
current are 0, therefore battery parameter/state estimation cannot
be conducted.

**B. Battery Parameter/State Identification**

Parameter/state identification of a battery was conducted in
simulation. A Samsung 18650 lithium-ion, introduced in [17],
is adopted in this article, and all battery current profiles are
scaled (the scale ratio is 0.08) to fit the single cell, whose
specifications are listed in Table II. As shown in Fig. 8, the
simulation is conducted based on the first-order ECM, whose
voltage is governed by the same dynamics as the adopted battery
cell [see (2) and (3)]. The coefficients \( K_0 - K_4 \) of the OCV–SoC
for the adopted cell are 2.6031, 0.0674, \(-1.527\), 0.6265, and
\(-0.0297\), respectively.

For a fair comparison, the initial guesses of the identi-
ﬁed parameters and states are the same for MPC+ and
MPC−, which are \([R_s(0) \ R_t(0) \ \tau(0) \ 1/Q_b(0) \ SoC_b(0)]^T =
[0.02 \Omega \ 0.01 \Omega \ 10 \ s \ 1/2 \ Ah^{-1} \ 50\%]^T\). The sequential algorithm is
used to identify the battery states/parameters based on the results
of MPC+. In Step #1, a ﬁrst-order butterworth high-pass ﬁlter
with 3 dB bandwidth of 0.1 Hz is chosen based on the current
characteristics shown in Fig. 7(b). The ohmic resistance \( R_s \) is
identiﬁed using the EKF. As shown in Fig. 9(a), the identi-
fied value can accurately track the actual value. In Step #2, a
ﬁrst-order butterworth high-pass ﬁlter is designed with a 3 dB
bandwidth of 0.008 Hz based on the result shown in Fig. 7(c).
The identiﬁed \( R_s \) obtained from Step #1 is used, therefore \( R_t \) and
\( \tau \) can be accurately identiﬁed by the EKF, as shown in Fig. 9(b).

In Step #3, based upon the above identiﬁed parameters, a
combined SoC and SoH identiﬁcation is conducted using the
dual EKF, which can estimate the parameters and states si-
multaneously. The detailed information about the sequential
algorithm can be found in [25]. This previous study showed
that the identiﬁcation of SoC and SOH does not inﬂuence each
other, and both prefer high OCV–SoC rate and current amplitude
[17]. In addition, the identiﬁcation of SoC is not inﬂuenced by
the current frequency, while the identiﬁcation of SoH prefers
low current frequencies [25]. As a result, no excitation current
needs to be injected and the battery current proﬁle derived from
MPC− can be used, which means that we switch from MPC+ to
MPC− in Step #3. As shown in Fig. 9(c), the identiﬁed SoC
follows the actual value accurately and the identiﬁcation error
is below 0.5%. In addition, the identiﬁed capacity converges to
the actual value after 150 s, as shown in Fig. 9(d).

Hence, a satisfactory SoC and SoH identiﬁcation performance
is achieved based on the parameters estimated in Step #1 and
Step #2, even though no excitation current is injected in Step #3.
It is validated that the battery parameter/state can be accurately
identiﬁed using the sequential algorithm and the SIC is well
addressed by the proposed MPC+.

In the comparison case, all parameters and states are identiﬁed
based on the MPC− results shown in Fig. 4. The multi-scale EKF,
which has been shown to be more effective than the dual EKF

<p>| Table II: Specifications for the 18650 Battery Cell |</p>
<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nominal Voltage (V)</td>
<td>3.63</td>
</tr>
<tr>
<td>Cell Capacity (Ah)</td>
<td>2.44</td>
</tr>
<tr>
<td>Ohmic Resistance ( R_s ) (mΩ)</td>
<td>100</td>
</tr>
<tr>
<td>Diffusion Resistance ( R_t ) (mΩ)</td>
<td>33</td>
</tr>
<tr>
<td>Time Constant ( \tau ) (s)</td>
<td>17</td>
</tr>
<tr>
<td>Discharge/Charge Efficiency ( \eta ) (%)</td>
<td>98</td>
</tr>
<tr>
<td>OCV–SoC slope ( a ) (mV/100%)</td>
<td>-8.845</td>
</tr>
</tbody>
</table>

Fig. 8. Simulation model of the first-order circuit.

Fig. 9. Parameter identiﬁcation result of MPC+. (a) \( R_s \) (Step #1). (b) \( R_t \) and \( \tau \) (Step #2). (c) SoC (Step #3). (d) \( Q_b \) (Step #3).
Fig. 10. Parameter identification result of MPC–. (a) $R_s$. (b) $R_t$ and $\tau$. (c) SoC. (d) $Q_b$.

Fig. 11. Battery terminal voltage comparison. (a) MPC+. (b) MPC–.

Fig. 12. Tradeoff between identification accuracy and system efficiency.

C. Tradeoff Between Identification and Optimization

As illustrated above, the proposed MPC+ improves identification accuracy at the expense of an increase in energy loss. To further investigate the tradeoff between identification and optimization, the amplitudes of the injected current (i.e., $I_{ex}$) are fixed at various values and MPC+ is used for the optimization. The ohmic resistance is identified based on simulation results and the root mean square (rms) of the identification error is calculated. The value of $I_{ex}$ ranges from 1 to 8 A, and the simulation results are shown in Fig. 12. This shows that the identification accuracy can be improved by increasing $I_{ex}$, which verifies the conclusion that the identification accuracy of battery parameters is related to the amplitude of the excitation current. However, energy loss also increases as $I_{ex}$ increases. It is worth noticing that the identification accuracy can be significantly improved initially with an increasing $I_{ex}$; however, the effect of increasing $I_{ex}$ on improving identification accuracy is not obvious for the $I_{ex}$ beyond a transition area, where the “knee” point (i.e., $I_{ex} = 6$ A) can be found and selected as the optimal solution [38].

Parameter identification is also significantly influenced by measurement noise. To verify the robustness of the optimal amplitude of excitation current, the noise amplitude (in the voltage measurement) is varied in the simulation, and the identification of $R_s$ is conducted under different levels of white noise. When the white noise amplitudes are 50% and 200% of the original value, the simulation results show similar trends when compared to the original result, as shown in Figs. 12 and 13. As a result, the optimal solution is robust to different noise levels.

Note that the rms error of $R_s$ corresponding to MPC- is 12.5 mΩ. In comparison, when $I_{ex}$ is 1 A the RMS error corresponding to MPC+ is 6.58 mΩ, indicating that the identification error can be reduced by 47.4% even when the injected current...
is small. Therefore, the active current injection realized by the proposed MPC+ can significantly reduce the identification errors of battery parameters. Due to space limitations, tradeoffs associated with identification of the $RC$ pair is not investigated here. We also note that the energy loss of MPC+ can be potentially reduced. As shown in Fig. 9, the identification of ohmic resistance and $RC$ pair only takes 200 and 50 s, respectively. If desired, the identification periods of Step #1 and Step #2 can be turned off, and so MPC+ can be switched to MPC– to further reduce energy loss. In addition, the proposed MPC+ can be generalized to other overactuated systems with batteries (e.g., hybrid electric vehicles) to simultaneously achieve identification and loss minimization objectives [39].

This article emphasizes how to implement the sequential algorithm in overactuated systems (e.g., battery/supercapacitor HESS), and no experimental validation is presented here. However, we point out that the effectiveness and robustness of the sequential algorithm have been experimentally validated in other works. The detailed information can be found in [17] and [25].

V. CONCLUSION

A novel MPC was proposed in this article for handling simultaneous identification and optimization of HESS using active current injection. The overactuated feature of HESS was exploited to achieve accurate identification of battery state/parameter and satisfactory system efficiency simultaneously. The proposed MPC approach simultaneously considers the system efficiency, injected signal richness, and output power regulation. Simulation results showed that when compared to the baseline MPC without considering active current injection, the proposed MPC can effectively perform the SIC. Specifically, the proposed MPC significantly improves the identification accuracy of battery parameter/state (e.g., the rms errors of the estimated $R_s$ and SoC can be both reduced by around 50%) at the expense of a slight increase in the energy consumption (i.e., around 0.4%). The tradeoff between identification accuracy and system efficiency was investigated and the optimal amplitude of the injected current, which achieves the best tradeoff and is robust to noise amplitude, was determined.

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